# Ship Behaviour in Shallow and Confined Water: an Overview of Hydrodynamic Effects through EFD









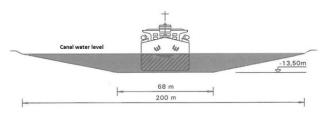
### Ship Behaviour in Shallow and Confined Water

- Shallow and confined water areas in Flanders
  - Canal Ghent-Terneuzen: interaction of maritime and inland fleet
  - Upper Sea-Scheldt: inland waterway
- Effect on ship behaviour
  - ship manoeuvring in open and shallow water
  - bank effects
  - ship-to-ship interaction
  - nautical bottom

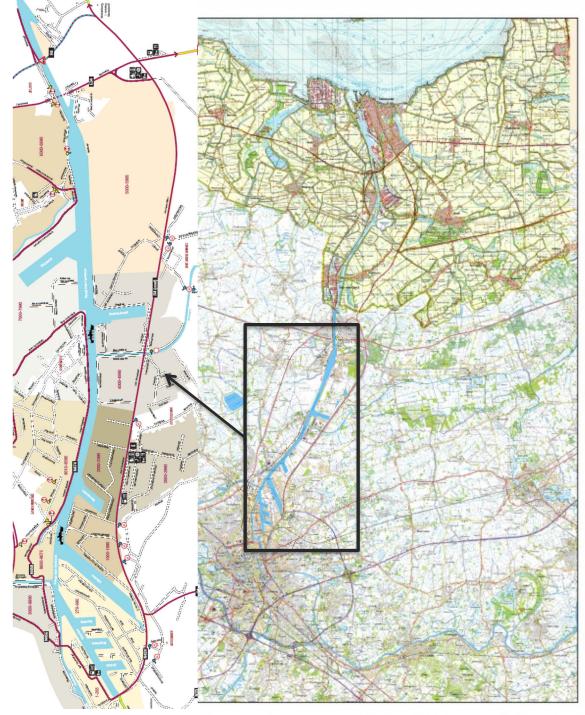


# **Canal Ghent- Terneuzen**





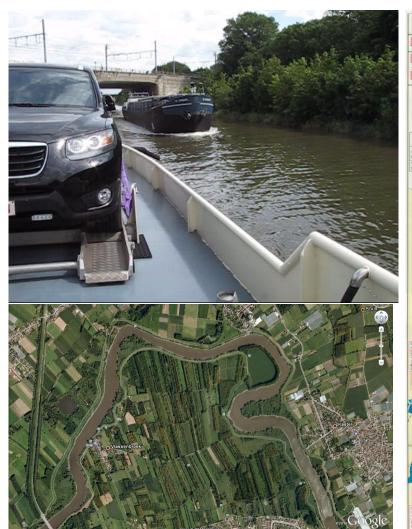
Designed for a panamax sized vessel increased to a beam of 37 m. 38 m is under investigation

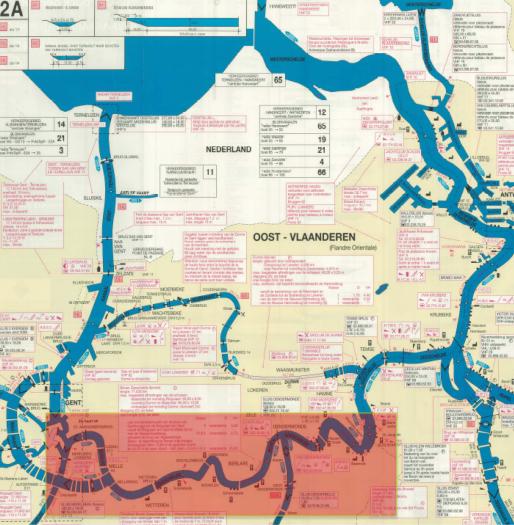






# **Upper Sea-Scheldt**









# Ship Behaviour in Shallow and Confined Water

- Shallow and confined water areas in Flanders
  - Canal Ghent-Terneuzen: interaction of maritime and inland fleet
  - Upper Sea-Scheldt: inland waterway

Port of Zeebrugge: nautical bottom – mud layer

above a solid bottom







# Ship Behaviour in Shallow and Confined Water

Towing tank for manoeuvres in shallow water (cooperation Flanders Hydraulics Research – Ghent University)









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used for

- admittance policy
- inland navigation





# Ship Behaviour in Shallow and Confined Water

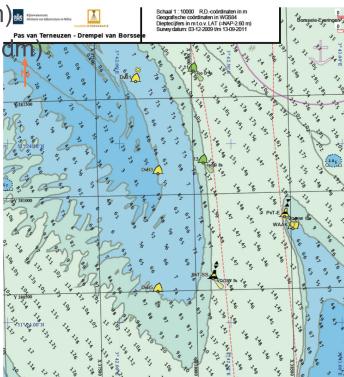
Effect on ship behaviour – video 38

18/04/2005 – Vlissingen – Springergeul

Lykes Motivator 243 m x 32 m (103 dm)

MSC Katherine Ann 184 m x 25 m (77

Zarechensk 180 m x 28 m (107 dm)







#### **Overview**

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- Literature review: manoeuvring performance
  - Ankudinov: "concept of modularity based on a separate representation of elements of the manoeuvring model"
  - Japan Towing Tank Committee: MMG model

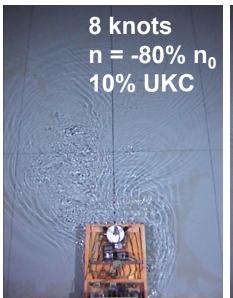




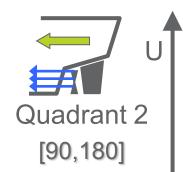


- Literature review: manoeuvring performance
  - Ankudinov
  - Japan Towing Tank Committee
  - Oltmann & Sharma, HSVA:

four quadrant concept









Quadrant 3 [-180,-90]



Quadrant 4 [-90,0]





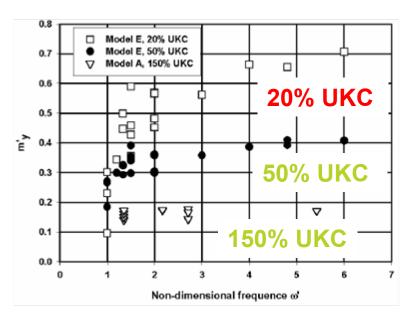


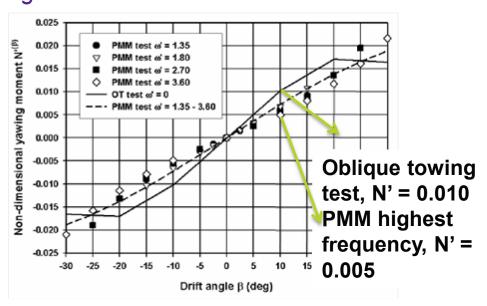
- Literature review: manoeuvring performance
  - Ankudinov
  - Japan Towing Tank Committee
  - Oltmann & Sharma, HSVA
  - Hydronautics Research: low speed manoeuvring models
  - Force Technology (DMI): look-up tables
  - Flanders Hydraulics Research: modular and tabular manoeuvring models (3 or 4 DOF) based on captive model tests and validated using free-running model tests and full scale measurements





- Model tests
  - Flanders Hydraulics Research: increasing influence of chosen test parameters during captive model tests on the derived mathematical model when UKC is decreasing





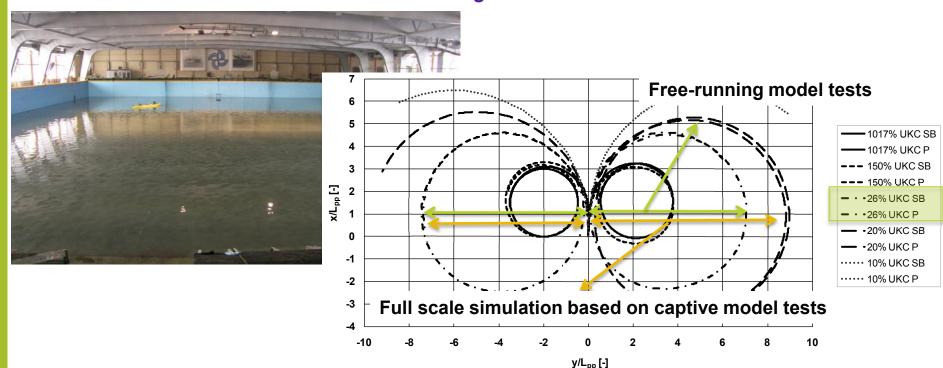
**Test frequency** 

**Test type** 





- Simulation model
  - Flanders Hydraulics Research: increasing influence of chosen test parameters during captive model tests on the derived mathematical model when UKC is decreasing







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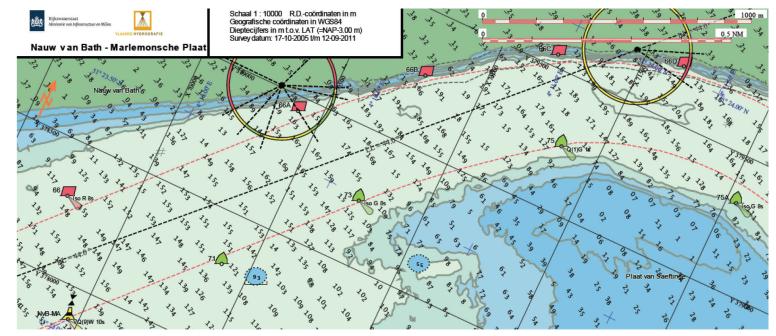
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Video







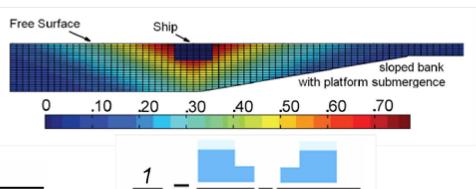


• Norrbin: "if the channel banks are not vertical walls but sloping beaches the definition of the bank distance parameter is less obvious.", work extended by Ch'ng, Doctors and Renilson

Which vertical reference height to measure the distance between a ship and a bank?

Other formulations for the hydrodynamic changes in the water flow due to the vicinity of banks

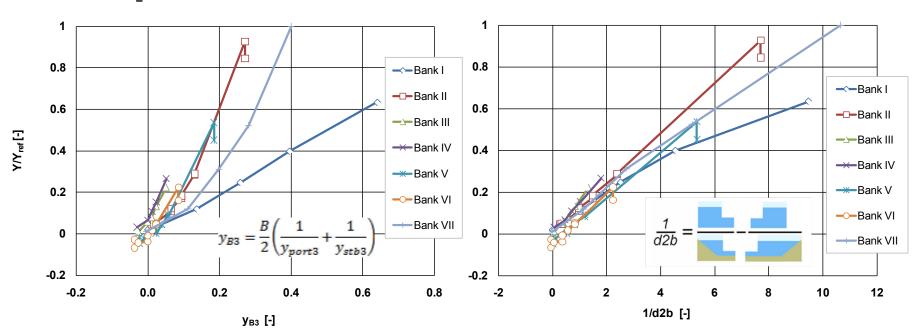
• FHR and UGent:  $d_{2b}$  and  $m_{eq}$  Weight distribution  $e^{-a|y|-b|z|}$ 



$$m_{eq} = \frac{1}{1 + 1} + \frac{1}{1 + 1}$$



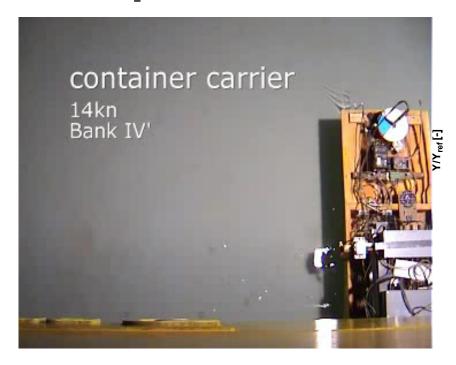


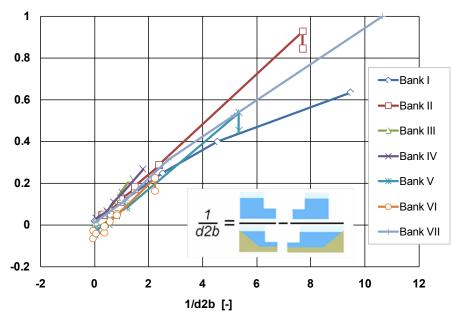


Container carrier at 10 knots and 100% UKC, no propeller





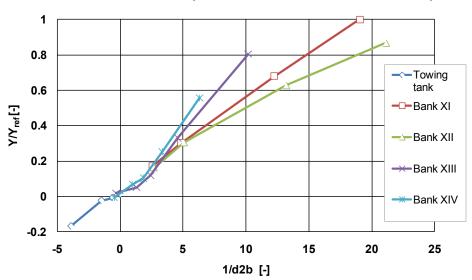








• KVLCC2 (10 knots, 50% UKC)









• KVLCC2



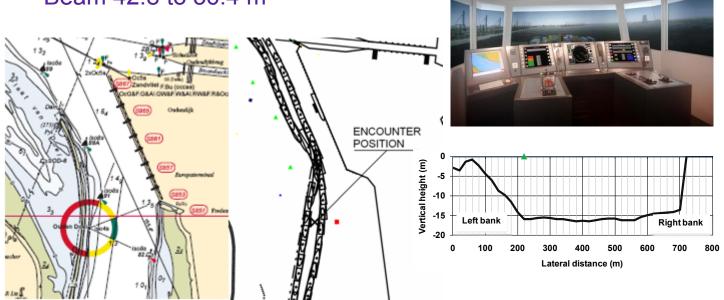






Real-time simulation study: meeting of two ULCS

Length 350 to 400 m Beam 42.8 to 56.4 m







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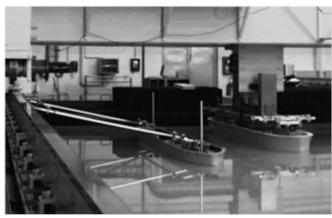


Knowledge Centre Manoeuvring in Shallow and Confined Water, Conference May 2011 hosted by NTNU and MARINTEK

- moored ships alongside quays;
- ships anchored or moored to buoys;
- ships meeting / passing on parallel / oblique / curved / steered paths;
- interaction with more than one ship or marine structure;
- ship-to-ship interaction during lightering operations;
- ship-to-ship interaction during tug assistance.











Meeting and overtaking

Lightering

Tug – ship interaction

Ship		С	D	Е	Н
$L_{pp}$	m	3.984	3.864	3.824	2.210
В	m	0.504	0.550	0.624	0.296
$T_{ref}$	m	0.180	0.180	0.207	0.178
$C_B$ (at $T_{ref}$ )	-	0.843	0.588	0.816	0.830
T	m	0.155 - 0.200	0.155 - 0.200	0.136 - 0.256	0.125 - 0.178





Project: KMB Investigating hydrodynamic aspect and control systems fot ship-to-ship operations, co-ordinated by MARINTEK and financially supported by the Research Council of Norway

- Zero longitudinal speed difference
- Special case of overtaking and overtaken
- Steady state and dynamic tests
- Open STS data

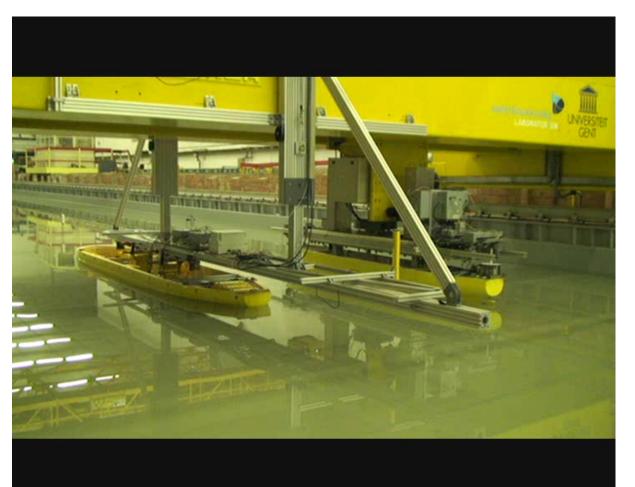


Lightering

h	$T_{STBL}$	$n_{\mathrm{STBL}}$	V	$T_{SS}$	$\psi_{SS}$	n <sub>SS</sub>	δу	δx
[m]	[m]	[-]	[kts]	[m]	[deg]	[-]	[m]	[m]
h <sub>max</sub>	20.8	selfprop	2.0	7.5	180	Slow	4	0
1.35 T <sub>STBL</sub>	12.8		4.0	15	179	Half	10	L/2
		1	5.0		178	selfprop	25	-L/2
			6.0		177		50	
			<u> </u>	I	175	1	100	









Lightering







#### Tug – ship interaction

Forward speed [knots], full scale	5, 6, 7, 8, 9
Longitudinal separation x' <sub>rel</sub> [-], from amidships of container vessel to centre of gravity of tug (non-dimensional value based on length of tug)	0.73, 1.25, 1.77, 2.29, 2.82, 3.33, 3.88, 4.41, 4.93
Transverse separation y' <sub>rel</sub> [-], from centreline to centreline (non-dimensional value based on breadth of tug)	2.6, 3.3, 4.0, 4.4, 5.3
Drift angle [°], negative angle bow-in since tug model is situated on starboard in the towing tank	-10, -5, 0, 5, 10







- Dedicated interaction models complex pressure field change
- Different methodic combinations as EFD, CFD or other numerical codes
- JIP ROPES, lead partner MARIN, Research on Passing Effects on Ships





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#### **Nautical bottom**

- PIANC: "nautical bottom as the level where physical characteristics of the bottom reach a critical limit beyond which contact with a ship's keel causes either damage or unacceptable effects on controllability and manoeuvrability"
  - Multidisciplinary approach: measuring/survey techniques, dredging techniques, physical mud characteristics, effect of mud layers on the behaviour of ships
  - EFD and nautical bottom research = how incorporate viscous effects if Reynold's law is not fulfilled? Mud layer is a homogeneous layer with constant density and rheological properties.





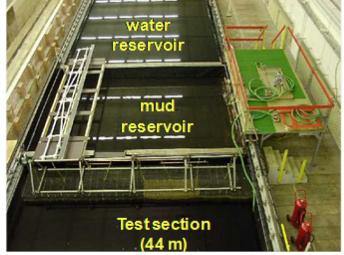
#### **Nautical bottom**

- Model tests at FHR
  - Layer thickness
  - Mud density
  - Mud viscosity
  - Under keel clearance



78 parameter combinations









#### **Nautical bottom**

- Results for the port of Zeebrugge
  - Density criterion is 1.2 ton/m³ instead of 1.15 ton/m³
  - Navigation through the mud (negative UKC's water-mud interface)
  - 300 m length container ship -7% UKC assisted by two 45 ton tugs
- Main causes for the effect of mud layers on ship manoeuvrability:
  - Internal wave pattern in the water-mud interface greatly depended on mud density
  - Rheological characteristics of the mud: (non –) Newtonian fluid
- Development of in situ survey techniques
  STT sediment test tank







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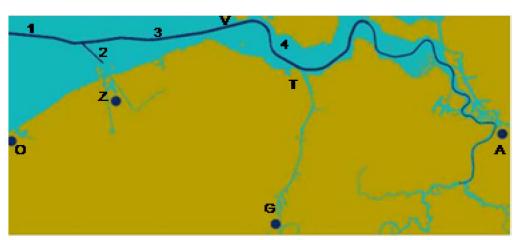




# **Example 1: admittance policy**

Admittance policy based on a certain window

- Tidal water level (min. gross UKC, % ship's draft):
  - 15% coastal channels 1, 3
  - 12.5% for 2 and 4 (Dutch part)
  - 10% for 4 (Belgian part) and Z outer harbour
  - 1 m for Sea Canal Terneuzen Ghent
- Current (Z: 2 kn 1.5 kn)
- Penetration in fluid mud (Z: 7%)







# **Example 1: admittance policy**

Admittance policy based on a gross UKC



Improved by a decision supporting tool ProToel:

- **Deterministic:** gross UKC (nautical bottom and top of fluid mud layers, lateral current component)
- **Probabilistic**: probability of bottom touch (due to squat and response to waves) < selected maximum value

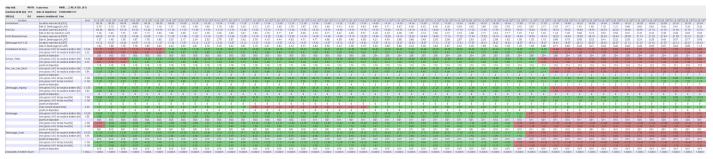
Used for long term and short term decisions for the maximum allowable draft

Evaluation phase by the Flemish Pilotage and Shipping Assistance Devision for the port of Zeebrugge





# **Example 1: admittance policy**



ship hull: W100 1	trajectory: KWBZ-All_K120_(	_(S1)																								
maximal draft [m]: 15.5	date of departure: 01/08/2008 CET																									
GM [m]: 0.0	waves considered: true																									
location		limit	8:15 CET	8:30 CET	8:45 CET	9:00 CET	9:15 CET	9:30 CET	9:45 CET	10:00 CET	10:15 CET	10:30 CET	10:45 CET	11:00 CET	11:15 CET	11:30 CET	11:45 CET	12:00 CET	12:15 CET	12:30 CE	T12:45 CET	13:00 CE*	T13:15 CE7	13:30 CET	T13:45 CET1	14:00 CET
Kwintebank	location reached at [CET]		08:24	08:39	08:54	09:09	09:24	09:39	09:54	10:09	10:24	10:39	10:54	11:09	11:24	11:39	11:54	12:09	12:24	12:39	12:54	13:09	13:24	13:39	13:54	14:09
	tide in Zeebrugge [m LAT]	,	0.70	0.70	0.78	0.85	1.05	1.16	1.37	1.45	1.58	1.64	1.78	1.86	2.03	2.13	2.34	2.46	2.78	2.97	3.42	3.66	4.15	4.35	4.63	4.69
PvhZ-SZ	location reached at [CET]		09:40	09:55	10:10	10:25	10:40	10:55	11:10	11:25	11:40	11:55	12:10	12:25	12:40	12:55	13:10	13:25	13:40	13:55	14:10	14:25	14:40	14:55	15:10	15:25
	tide in Bol van Heist [m LAT]	,	1.29	1.44	1.55	1.65	1.73	1.84	1.96	2.08	2.22	2.38	2.56	2.80	3.07	3.40	3.76	4.11	4.41	4.60	4.70	4.71	4.67	4.60	4.51	4.39
PvhZ-Strekdammen	location reached at [CET]		09:55	10:10	10:25	10:40	10:55	11:10	11:25	11:40	11:55	12:10	12:25	12:40	12:55	13:10	13:25	13:40	13:55	14:10	14:25	14:40	14:55	15:10	15:25	15:40
	tide in Zeebrugge [m LAT]		1.37	1.49	1.58	1.67	1.78	1.90	2.03	2.17	2.34	2.53	2.78	3.07	3.42	3.79	4.15	4.44	4.63	4.71	4.71	4.66	4.58	4.48	4.36	4.21
Zeebrugge A2 K120	location reached at [CET]		10:12	10:27	10:42	10:57	11:12	11:27	11:42	11:57	12:12	12:27	12:42	12:57	13:12	13:27	13:42	13:57	14:12	14:27	14:42	14:57	15:12	15:27	15:42	15:57
	tide in Zeebrugge [m LAT]		1.52	1.58	1.70	1.78	1.95	2.03	2.23	2.34	2.61	2.78	3.18	3.42	3.91	4.15	4.51	4.63	4.72	4.71	4.63	4.58	4.44	4.36	4.15	4.04
Kwintebank-Scheur	min gross UKC to nautical bottom [%]		11.77	12.07	12.71	13.16	14.23	14.81	15.98	16.59	17.79	18.37	19.49	20.07	21.35	22.08	23.78	24.79	27.12	28.43	31.09	32.31	34.22	34.85	35.00	34.62
	min gross UKC to nautical bottom [m]	2.32	1.82	1.87	1.97	2.04	2.21	2.30	2.48	2.57	2.76	2.85	3.02	3.11	3.31	3.42	3.69	3.84	4.20	4.41	4.82	5.01	5.30	5.40	5.42	5.37
	point on trajectory		200	500	500	500	500	500	500	500	500	500	500	500	500	500	500	500	500	500	500					7
Scheur_West	min gross UKC to nautical bottom [%]		12.96	13.95	14.85	15.63	1 48	16.93	17.64	18.41	19.26	20.16	21.23	22.50	24.08	25.96	28.13	30.39	32.48	34.19	35.23	0.5				_1
	min gross UKC to nautical bottom [m]	2.32	2.01	2.16	2.30	2.42	2.52	2.62	2.73	2.85	2.99	3.12	3.29	3.49	3.73	4.02	4.36	4.71	5.03	5.30	5.46	( ; r)	റടട	. CU	rrer	וו.
	point on trajectory	'	110	110	110	110	110	1,10	110	110	110	110	110	110	110	110	110	110	111	110	110	0.	500	00.	. 1 01	10
Pas_van_het_Zand	min gross UKC to nautical bottom [%]		14.12	15.07	15.83	16.42	16.99	17.67	18.43	10.05	20.42	24.46	22.24	22.04	25.04	27.74	20.05	22.24	24.24	25.40	36.15					
	min gross UKC to nautical bottom [m]	1.94	2.19	2.34	2.45	2.55	2.63	2.74	2.79					11.66					1.1		5.60	5.59	5 21	5.45	5.29	5.19
	point on trajectory		7	7	7	7	7	5	7	I\ /¹	lin (	arog	20 I	IK(	n	auti	ICal	hc	vtto.	m '	7	4	1	4	1	2
	min gross UKC to top mud [%]	-7.00	14.12	15.07	15.83	16.42	16.99	17.67	18.43	IV	шіў	JIO	33 L	ノバン	J 11'	aut	Cai		ILLUI	4 II - 7	36.15	36.06	35.54	35.13	34.12	33.48
	min gross UKC to top mud [m]	-1.08	2.19	2.34	2.45	2.55	2.63	2.74	2.86												5.60	5.59	5.51	5.45	5.29	5.19
	point on trajectory	'	7	7	7	7	7	5	7	7	7	6	7	6	7	6	7	6	7	7 '	7	4	1	4	1 1	2
Zeebrugge_Ingang	min gross UKC to nautical bottom [%]	12.50	14.84	15.61	16.18	16.75	17.49	18.29	19.13	20.03	21.08	22.34	23.92	25.80	28.04	30.45	32.76	34.68	35.85	36.41	36.36	3,103	35.54	34.93	34.12	33.14
	min gross UKC to nautical bottom [m]	1.94	2.30	2.42	2.51	2.60	2.71	2.84	2.96	3.10	3.27	3.46	3.71	4.00	4.35	4.72	5.08	5.38	5.56	5.64	5.64	5.59	5.51	5.41	5.29	5.14
	point on trajectory		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	min gross UKC to top mud [%]	-7.00	14.84	15.61	16.18	16.75	17.49	18.29	19.13	20.03	21.08	22.34	23.92	25.80	28.04	30.45	32.76	34.68	35.85	36.41	36.35	36.03	35.54	34.93	34.12	33.14
	min gross UKC to top mud [m]	-1.08	2.30	2.42	2.51	2.60					27	3.46	3.71	4.00	4.35	4.72	5.08	5.38	5.56	5.64	1	5.59	5.51	5.41	5.29	5.14
	point on trajectory		0	0	0	0	$\square$	had	roti	00	)	0	0	0	0	0	0	0	0	0	-0	0	0	0	0	0
	max current speed [knts]	2.00	1.41	1.31	1.22	1.12	Pe	net	Tau	OH	¥5 ;	0.58	0.92	1.40	1.99	2.58	3.04	3.33	3.35	3.21	2.96	2.69	2.43	2.21	2.03	1.86
	point on trajectory		0	0	0	0			,		)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
Zeebrugge	min gross UKC to nautical bottom [%]	10.00	10.86	11.29	1200	12.47	1.0 /	CI:	٠	اميد	.38	18.33	20.63	22.01	25.12	26.73	29.56	30.61	31.75	31.85	31.36	31.02	30.16	29.60	28.26	27.52
	min gross UKC to nautical bottom [m]	1.55	1.68	1.75	1.87	1.93	ın 7	fluid	n r	II IO	69	2.84	3.20	3.41	3.89	4.14	4.58	4.74	4.92	4.94	4.86	4.81	4.67	4.59	4.38	4.27
	point on trajectory		600	P '3	600	600		IGIC	J 111	uu	)0	600	600	600	601	600	600	600	600	610	611	601	611	601	611	601
	min gross UKC to top mud [%]	-7.00	-7.21	-6.40	-6.02	-5.09					68	1.34	2.57	5.46	7.06	10.18	11.50	13.27	13.68	13.78	13.29	12.95	12.09	11.54	10.20	9.45
	min gross UKC to top mud [m]	-1.08	-1.12	-0.99	-0.93	-0.79	-0.71	-0.54	-0.44	-0.23	-0.11	0.21	0.40	0.85	1.09	1.58	1.78	2.06	2.12	2.14	2.06	2.01	1.87	1.79	1.58	1.47
									601	601	601	610	601	601	601	601	601	601	601	610	611	601	611	601	611	601
	point on trajectory		601	610	601	610	601	601																		
Zeebrugge_Kaai	min gross UKC to nautical bottom [%]	10.00	11.29	11.67	12.47	12.97	14.05	14.61	15.85	16.56	18.33	19.41	22.01	23.52	26.73	28.25	30.61	31.33	31.91	31.85	31.36	31.02	30.16	29.60	28.26	27.52
Zeebrugge_Kaai	min gross UKC to nautical bottom [%] min gross UKC to nautical bottom [m]		11.29 1.75	11.67 1.81	12.47 1.93	12.97 2.01	14.05 2.18	14.61 2.26	15.85 2.46	16.56 2.57	2.84	3.01	3.41	3.65	4.14	4.38	4.74	4.86	4.95	4.94	4.86	4.81	4.67	4.59	4.38	4.27
Zeebrugge_Kaai	min gross UKC to nautical bottom [%] min gross UKC to nautical bottom [m] point on trajectory	10.00 1.55	11.29 1.75 615	11.67 1.81 615	12.47 1.93 615	12.97 2.01 615	14.05 2.18 615	14.61 2.26 615	15.85 2.46 615	16.56 2.57 615	2.84 615	3.01 615	3.41 615	3.65 615	4.14 615	4.38 615	4.74 615	4.86 615	4.95 615	4.94 615	4.86 615	4.81 615	4.67 615	4.59 615	4.38 615	4.27 615
Zeebrugge_Kaai	min gross UKC to nautical bottom [%] min gross UKC to nautical bottom [m] point on trajectory min gross UKC to top mud [%]	10.00 1.55 -7.00	11.29 1.75 615 -6.77	11.67 1.81 615 -6.40	12.47 1.93 615 -5.59	12.97 2.01 615 -5.09	14.05 2.18 615 -4.02	14.61 2.26 615 -3.45	15.85 2.46 615 -2.22	16.56 2.57 615 -1.50	2.84 615 0.26	3.01 615 1.34	3.41 615 3.95	3.65 615 5.46	4.14 615 8.66	4.38 615 10.18	4.74 615 12.55	4.86 615 13.27	4.95 615 13.84	4.94 615 13.78	4.86 615 13.29	4.81 615 12.95	4.67 615 12.09	4.59 615 11.54	4.38 615 10.20	4.27 615 9.45
Zeebrugge_Kaai	min gross UKC to nautical bottom [%] min gross UKC to nautical bottom [m] point on trajectory min gross UKC to top mud [%] min gross UKC to top mud [m]	10.00 1.55	11.29 1.75 615 -6.77 -1.05	11.67 1.81 615 -6.40 -0.99	12.47 1.93 615 -5.59 -0.87	12.97 2.01 615 -5.09 -0.79	14.05 2.18 615 -4.02 -0.62	14.61 2.26 615 -3.45 -0.54	15.85 2.46 615 -2.22 -0.34	16.56 2.57 615 -1.50 -0.23	2.84 615 0.26 0.04	3.01 615 1.34 0.21	3.41 615 3.95 0.61	3.65 615 5.46 0.85	4.14 615 8.66 1.34	4.38 615 10.18 1.58	4.74 615 12.55 1.94	4.86 615 13.27 2.06	4.95 615 13.84 2.15	4.94 615 13.78 2.14	4.86 615 13.29 2.06	4.81 615 12.95 2.01	4.67 615 12.09 1.87	4.59 615 11.54 1.79	4.38 615 10.20 1.58	4.27 615 9.45 1.47
Zeebrugge_Kaai	min gross UKC to nautical bottom [%] min gross UKC to nautical bottom [m] point on trajectory min gross UKC to top mud [%] min gross UKC to top mud [m] point on trajectory	10.00 1.55 -7.00 -1.08	11.29 1.75 615 -6.77 -1.05 615	11.67 1.81 615 -6.40	12.47 1.93 615 -5.59	12.97 2.01 615 -5.09	14.05 2.18 615 -4.02	14.61 2.26 615 -3.45	15.85 2.46 615 -2.22	16.56 2.57 615 -1.50	2.84 615 0.26	3.01 615 1.34	3.41 615 3.95 0.61 615	3.65 615 5.46	4.14 615 8.66	4.38 615 10.18 1.58 615	4.74 615 12.55 1.94 615	4.86 615 13.27	4.95 615 13.84	4.94 615 13.78	4.86 615 13.29	4.81 615 12.95	4.67 615 12.09 1.87 615	4.59 615 11.54	4.38 615 10.20 1.58 615	4.27 615 9.45





#### **Overview**

### Ship Behaviour in Shallow and Confined Water

- Shallow and confined water areas in Flanders
- Effect on ship behaviour
  - ship manoeuvring in open and shallow water
  - bank effects
  - ship-to-ship interaction
  - nautical bottom

used for

- admittance policy
- inland navigation



# **Example 2: inland navigation**

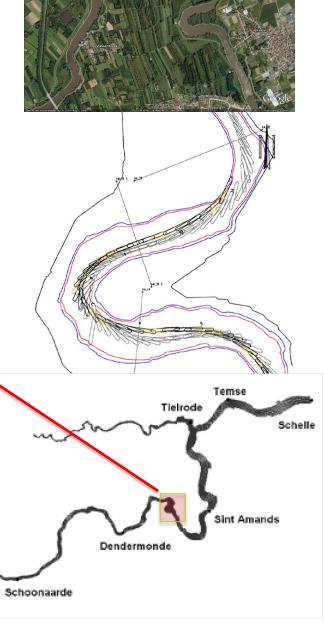
Melle

Merelbeke

Wetteren

Design criteria for inland transport







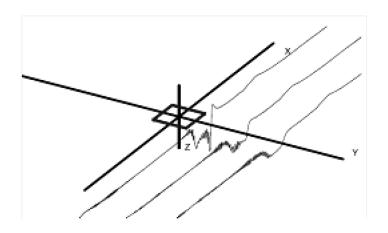


# **Example 2: inland navigation**

Simulation model based on captive model tests

- Ship manoeuvring in shallow water
- Bank effects
- STS interaction module

based on generalised model for maritime ships





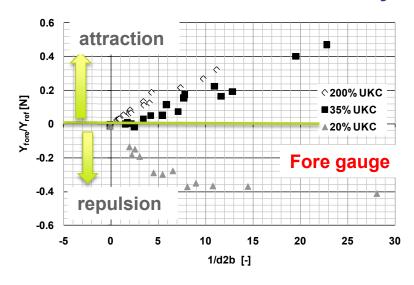


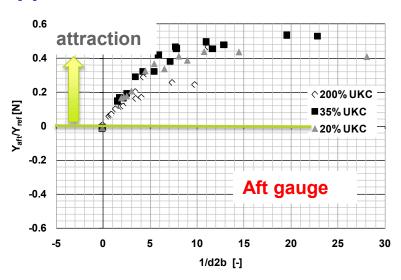


# **Example 2: inland navigation**

#### Validation

- Multimodal captive model tests
- Free-running model tests
- Full scale measurements during trial voyages
- Real-time simulation by a skipper on the inland simulator Lara





Lateral force due to bank effects at fore and aft gauges





# **Summary**

- Ship manoeuvrability decreases for UKC < 50% draft</li>
- Complex hydrodynamic effects due to horizontal (bank, ship) and vertical (shallow water, nautical bottom) restrictions
- Knowledge based on different methodologies
  - Experimental fluid dynamics (force water flow)
  - Computational fluid dynamics (pressure water flow)
  - Numerical methods
- Co-operation